

2) Given: $D = 30 \text{ in}$
 $p = 14.4 \text{ psig}$

$$p = \frac{F}{A}$$

$$A = \frac{\pi D^2}{4}$$

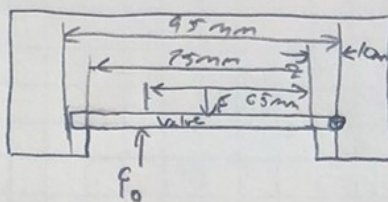
$$F = pA$$

$$A = \frac{\pi (30)^2}{4}$$

$$F = (14.4)(706.858) \quad A = 706.858 \text{ in}^2$$

$$F = 10178.755 \text{ lb}$$

10) Given: $D = 500 \text{ mm}$
 $h = 1.8 \text{ m}$
 $d = 75 \text{ mm}$



$$F = pA \rightarrow \textcircled{1}$$

$$D = 10 + 75 + 10$$

$$D = 95 \text{ mm or } 0.095 \text{ m}$$

$$A = \frac{\pi D^2}{4}$$

$$= \frac{\pi}{4} (0.095)^2$$

$$A = 7.088 \times 10^{-3} \text{ m}^2$$

$$p = \gamma h$$

$$= 9.81 \text{ kN/m}^3 (1.8 \text{ m})$$

$$p = 17.658 \text{ kN/m}^2$$

$$F = (17.658 \text{ kN/m}^2)(7.088 \times 10^{-3} \text{ m}^2)$$

$$F = 0.125 \text{ kN}$$

$$\sum M_{\text{hinge}} = 0$$

$$125 \left(\frac{95}{2} \right) - F_0 (65) = 0$$

$$F_0 = 91.35 \text{ N}$$

17) Given: $S_g = 0.8$
 $l = 4\text{ m}$
 $h = 1.4\text{ m}$
 $\theta = 45^\circ$

$$p = \frac{F_A}{A}$$

$$F_A = pA \quad \leftarrow \quad p = \gamma_0 h_c$$

$$F_A = \gamma \left(\frac{h}{2} \right) A$$

$$F_A = (8.436) \left(\frac{1.4}{2} \right) (7.919)$$

$$F_A = 46.76 \text{ kN}$$

$$\frac{h}{3} = \frac{1.4}{3}$$

$$h_3 = 0.466\text{ m}$$

$$\frac{L}{3} = \frac{1.979}{3}$$

$$\frac{L}{3} = 0.659\text{ m}$$

$$L_p = L - \frac{L}{3}$$

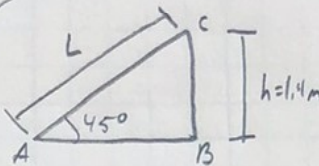
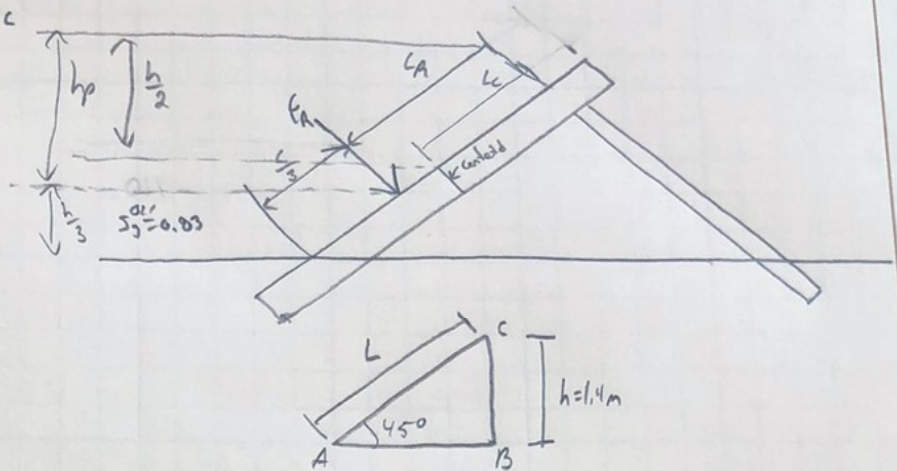
$$L_p = 1.979 - 0.659$$

$$L_p = 1.32\text{ m}$$

$$h_p = h - \frac{h}{3}$$

$$h_p = 1.4 - 0.466$$

$$h_p = 0.934\text{ m}$$



$$\sin \theta = \frac{h}{L}$$

$$L = \frac{h}{\sin \theta}$$

$$L = \frac{1.4}{\sin 45^\circ}$$

$$L = 1.979\text{ m}$$

$$A = L(\sin \theta)$$

$$A = 1.979(4)$$

$$A = 7.919\text{ m}^2$$

$$\gamma = (0.8)(9.801)$$

$$\gamma = 8.436 \text{ kN/m}^3$$

Homework Chapter 5

Problem 5.8

Given;

Specific gravity of oil = 0.90

Total weight of pump = 14.6 lb

Submerged volume = 40 in³

$$F_b = \gamma_f V_d$$

$$S_g = \frac{\gamma_f}{62.4 \text{ lb/ft}^3}$$

$$\therefore \gamma_f = 0.90 \times 62.4 \text{ lb/ft}^3$$

$$\gamma_f = 56.16 \text{ lb/ft}^3$$

$$F_b = \gamma_f V_d$$

$$F_b = (56.16)(0.0232)$$

$$F_b = 1.3029 \text{ lb}$$

$$\sum F_v = 0$$

$$F_b - W + F_r = 0$$

$$F_r = W - F_b$$

$$F_r = 14.6 - 1.3029$$

$$F_r = 13.297 \text{ lb}$$

$$\therefore \text{exerted force, } F_r = \underline{13.297 \text{ lb}}$$

Problem 5.24

Given:

$$D = 750 \text{ mm} = 0.75 \text{ m}$$

$$h = 750 \text{ mm} = 0.75 \text{ m}$$

$$T = 95^\circ \text{C}$$

Specific weight of water 95°C is $\gamma_f = 9.44 \text{ kN/m}^3$
 $\gamma_c = 6.45 \text{ kN/m}^3$ placed 95°C

$$F_b = \gamma_f V_c$$

$$w = \gamma_c V$$

$$\text{Volume } V_c = \frac{\pi}{4} D^2 h = \frac{\pi}{4} (0.75)^2 (0.75) = 0.1193 \text{ m}^3$$

$$V_b = \frac{\pi}{4} D^2 h$$

$$= \frac{\pi}{4} (0.75)^2 (t)$$

$$= 0.159t \text{ m}^3$$

$$V = 0.1193 + 0.159t$$

$$\sum F_r = 0$$

$$F_b - w_c - w_b = 0$$

$$F_b = w_c + w_b$$

$$9.44 \times (0.1193 + 0.159t) = [6.45 \times 0.1193] + [84.0 \times 0.159t]$$

$$t = \frac{0.3567}{11.855}$$

$$= 0.03 \text{ m}$$

$$\Rightarrow 30 \text{ mm}$$

$$\therefore t = \underline{\underline{30 \text{ mm}}}$$

Problem 5.41

Given:

$$w = 450000 \text{ lb}$$

$$H = 8 \text{ ft}$$

$$B = 20 \text{ ft}$$

$$L = 50 \text{ ft}$$

$$\text{Center of gravity} = 8 \text{ ft}$$

$$V = 64 \text{ lb/ft}^2$$

$$V_d = (1000)(7.03)$$

$$V_d = 7030 \text{ ft}^3$$

$$I = \frac{LB^3}{12}$$

$$= \frac{(50)(20)^3}{12}$$

$$= 33.33 \times 10^3 \text{ ft}^4$$

$$F_b = r_f V_d$$

$$V_d = LBH$$

$$= 50 \times 20(x)$$

$$V_d = 1000(x)$$

$$\therefore V_d = 1000(x) \text{ ft}^3$$

$$MB = \frac{I}{V_d}$$

$$= \frac{33.33 \times 10^3}{7030}$$

$$MB = 4.742 \text{ ft}$$

$$F_b = V_f V_d$$

$$F_b = 64 \times 1000(x)$$

$$F_b = 64000(x) \text{ lb}$$

$$y_{mc} = y_{cb} + MB$$

$$= 3.515 + 4.742 \text{ ft}$$

$$y_{mc} = 8.257 \text{ ft}$$

$$F_b = w$$

$$64000(x) = 450000$$

$$x = \frac{450000}{64000}$$

$$x = 7.03 \text{ ft}$$

$$y_{cb} = \frac{x}{2}$$

$$= \frac{7.03}{2} = 3.515 \text{ ft}$$

$$\therefore y_{mc} = \underline{\underline{8.257 \text{ ft}}}$$

$$F_b = 64000(x)$$

$$= 64000(7.03)$$

$$F_b = \underline{\underline{450000 \text{ lb}}}$$

Q 5.61

①

Given

$$\text{Boat width} = W_{\text{Boat}} = 2.4 \text{ m}$$

$$\text{Boat length} = L_B = 5.5 \text{ m}$$

To Find:

$$\text{Boat stable} = ?$$

Solutions

$$\begin{aligned} \text{Rectangular Area of Boat} &= B_{\text{Rec}} = \frac{(1.5 - 0.6 + 0.3)}{2} \times 2.4 \\ &= (1.2) \times 2.4 = 2.88 \text{ m}^2 \end{aligned}$$

$$\begin{aligned} \text{Triangular Area of Boat} &= B_{\text{Tri}} = \frac{1}{2} \times 2.4 \times 0.6 \\ &= 0.72 \text{ m}^2 \end{aligned}$$

$$\begin{aligned} \text{Total Area of Boat} &= B_T = 2.88 + 0.72 \\ &= 3.6 \text{ m}^2 \end{aligned}$$

$$\text{Submerged Area As submerged} = A_{\text{Rec}} + A_{\text{Tri}}$$

$$= (0.9 \times 2.4) + \left(\frac{1}{2} \times 2.4 \times 0.6\right)$$

$$\begin{aligned} A_{\text{sub}} &= 2.16 + 0.72 \\ &= 2.88 \text{ m}^2 \end{aligned}$$

As we know that

(2)

$$\begin{aligned}\text{Centroid of full Area} &= \bar{y}_c = \frac{A_1 \bar{y}_1 + A_2 \bar{y}_2}{A_{\text{total}}} \\ &= \frac{(\frac{1}{2} \times 2.4 \times 0.6) \times \frac{2h}{3} + (1.2 \times 2.4) (0.6 + \frac{1.2}{2})}{3.6} \\ &= \frac{(0.72 \times 2 \times 0.6) / 3 + (2.88 \times 1.2)}{3.6} \\ &= \frac{0.288 + 3.456}{3.6} = 1.04 \text{ m}\end{aligned}$$

Now Find

Centroid of Submerged Area

$$\begin{aligned}\bar{y}_c &= \frac{A_1 \bar{y}_1 + A_2 \bar{y}_2}{A_{\text{sub}}} \\ &= \frac{(\frac{1}{2} \times 2.4 \times 0.6) \times \frac{2h}{3} + (0.9 \times 2.4) (0.6 + \frac{0.9}{2})}{2.88} \\ &= \frac{(0.72 \times 0.4) + (2.16)(1.05)}{2.88} \\ &= \frac{0.288 + 2.268}{2.88} = 0.8875 \text{ m}\end{aligned}$$

Now;

Total displaced volume

$$\begin{aligned}V_d &= A_{\text{sub}} \times B \\ &= 2.88 \times 5.5 \\ V_d &= 15.84 \text{ m}^3\end{aligned}$$

Now;

Moment of inertia = ?

$$I = \frac{B H^3}{12} = \frac{5.5 \times (2.4)^3}{12} = 6.335 \text{ m}^4$$

Central Height from Buoyancy center (3)

$$MB = \frac{I}{Vd}$$

$$MB = \frac{6.336}{15.84}$$

$$MB = 0.4m$$

Now

Center distance from the Base of the Boat

$$Y_{mc} = Y_c + MB$$

$$= 0.8875 + 0.4$$

$$\boxed{Y_{mc} = 1.2875m}$$

Center of Gravity, $Y_{cg} = 1.04m$

Now we can see

Metacenter is above the center of Gravity

$$Y_{mc} > Y_{cg}$$

Thus, The Boat is stable.

homework 28, 42, 54 ch 4

$$28) y = \frac{4R}{3\pi} \quad y = \frac{4(20)}{3\pi} = 8.49 \text{ in}$$

$$F_y = 8 + \bar{y}$$

$$8 + 8.49 = 16.49 \text{ in}$$

$$\cos 30^\circ = \frac{FE}{AF}$$

$$AF = \frac{10}{\cos 30^\circ} = 11.55 \text{ in}$$

$$L_c = AF + FG$$

$$11.55 + 16.49 = 28.04 \text{ in}$$

$$h_c = L_c \cos 30^\circ = 24.28 \text{ in}$$

$$y = SG \times y$$

$$y = 1.1 \times 62.4 = 68.64 \text{ lb/ft}^3$$

$$F_R = PA$$

$$= y h_c \times \left(\frac{\pi}{2} R^2 \right)$$

$$F_R = 68.64 \frac{\text{lb}}{\text{ft}^3} \times \left(24.28 \text{ in} \times \frac{1}{12} \right) \times \frac{\pi}{2} \left(\frac{20 \times \frac{1}{12}}{2} \right)^2$$

$$F_R = 605.916$$

$$I_c = \left(\frac{\pi}{8} - \frac{8}{9\pi} \right) R^4 = 17561.1 \text{ in}^4$$

$$L_p = L_c + \frac{I_c}{L_c A} \quad \text{or} \quad L_c + \frac{I_c}{L_c \left(\frac{\pi}{2} \cdot 20^2 \right)} = L_p = 29.02 \text{ in}$$

$$L_p - L_c = 29.02 - 28.04 = .98 \text{ in}$$

$$42) y = \frac{D}{2} \cos \theta$$

$$y = \frac{10}{2} \cos 30^\circ = 4.33 \text{ in}$$

$$L_c = \frac{h_c}{\cos \theta} = 48.87 \text{ in}$$

$$h_c = 38 + y$$

$$h_c = 42.33 \text{ in}$$

$$A = \frac{\pi \times 10^2}{4} = 78.54 \text{ in}^2$$

$$F_R = \gamma h_c A \quad F_R = 62.4 \times \left(\frac{42.33}{12} \right) \times \left(\frac{78.54}{12^2} \right) = 120.0516$$

$$I_c = \frac{\pi \times 10^4}{64} = 490.87 \text{ in}^4$$

$$h_p - h_c = \frac{490.87}{(48.87 \times 78.54)} = .128 \text{ in}$$

$$\sum M_H = 0 \quad F_R \times \left[\frac{D}{2} + (h_p - h_c) \right] - \left(F_c \times \frac{D}{2} \right) = 0$$

$$120.05 \cdot \left(\frac{10}{2} + .128 \right) - \left(F_c \times \frac{10}{2} \right) = 0$$

$$F_c = 123.1216$$

54)

$$h_1 = 48 \text{ in}$$

$$D = 36 \text{ in}$$

$$S_g = .78$$

$$w = 60 \text{ in}$$

$$A = \frac{\pi (36)^2}{8}$$

$$A = 508.93 \text{ in}^2$$

$$V = AW = 508.93 \cdot 60 = 30535.8 \text{ in}^3$$

$$y = S_g \cdot 62.4$$

$$y = (.78)(62.4) = 48.296 \text{ lb/ft}^3$$

$$w = yV = 48.296 \cdot 17.67$$

$$F_v = 871.06 \text{ lb}$$

$$x = .212 \cdot 36$$

$$= \bar{x} = 7.632 \text{ in}$$

$$h_c = 48 + \frac{36}{2}$$

$$h_c = 66 \text{ in}$$

$$F_H = y_s w h_c$$

$$48.296 \cdot 3 \cdot 5 \cdot 5.5 = F_H = 4066.92 \text{ lb}$$

$$5.5 + \frac{(3)^2}{(12)(5.5)}$$

$$h_p = 5.63 \text{ ft}$$

$$F_R = \sqrt{F_v^2 + F_H^2}$$

$$\sqrt{(871.06)^2 + (4066.92)^2}$$

$$= F_R = 4159.156 \text{ lb}$$

$$\phi = \tan^{-1}(F_v/F_H)$$

$$\tan^{-1}(871.06/4066.92)$$

$$\phi = 12.09^\circ$$

In class we started to look at the flow through a fitting. We learned you have weight to add to the equation. If we know one of the pressures on either side of the pipe we can still use Bernoulli's equation to find the other. Also we looked at if the pipe was a straight pipe. In this case you have no weak points such as flanges. We learned you have a R_y and R_x to solve for but not a R_z , therefore the two sides of the pipe push in opposite directions so they cancel one another out. Simply what's going on in the middle has the exact same on the side of the pipe also.